

Question Paper Code: 50838

B.E./B.Tech. DEGREE EXAMINATIONS, APRIL/MAY 2023.

Fourth/Fifth/Sixth Semester

Civil Engineering

MA 8491 – NUMERICAL METHODS

(Common to: Aeronautical Engineering/Aerospace Engineering/
Agriculture Engineering/Electrical and Electronics Engineering/Electronics and
Instrumentation Engineering/Instrumentation and Control
Engineering/Manufacturing Engineering/Mechanical Engineering
(Sandwich)/Mechanical and Automation Engineering/Biotechnology and
Biochemical Engineering/Chemical Engineering/Chemical and Electrochemical
Engineering/Plastic Technology/Polymer Technology/Textile technology)

(Regulations 2017)

Time: Three hours

Maximum: 100 marks

Answer ALL questions.

PART A —
$$(10 \times 2 = 20 \text{ marks})$$

- 1. What is the First iteration approximate solution of the equation 4x + y = 8 and 2x + 3y = 7 solved by Gauss Jacobi Method?
- 2. Find all eigen values of the matrix A by Jacobi's method where $A = \begin{pmatrix} 2 & -3 \\ -3 & 2 \end{pmatrix}$.
- 3. Form the divided difference table for the following data:

- y: 48 100 294 900
- 4. Find the Lagrange's interpolating polynomial passing through the points (0,0),(1,1),(2,20).
- 5. Evaluate $\int_{-1}^{1} \frac{dx}{1+x^2}$ by using two-point Gaussian quadrature formula.

6. Find $\frac{dy}{dx}$ of x = 50 by using the following Forward difference

$$x$$
 y Δy $\Delta^{2}y$

- 7. Using Euler's method, find y at x = 0.1 if $\frac{dy}{dx} = 1 + xy$, y(0) = 2.
- 8. State the Milne's predictor and corrector formula for solving differential equation numerically.
- 9. Write the finite difference scheme for $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 y}{\partial y^2} = 8x^2y^2$ for a square region with mesh size $\Delta x = \Delta y = 1$.
- 10. Write the explicit formula for one-dimensional wave equation if $1 \lambda^2 \alpha^2 = 0$ and $\lambda = \frac{k}{h}$.

PART B —
$$(5 \times 16 = 80 \text{ marks})$$

- 11. (a) (i) Find a real root of the equation $\cos x = 3x 1$ correct to three decimal places by iteration method. (6)
 - (ii) Find the largest Eigen value and its corresponding Eigen vector of

the matrix
$$A = \begin{pmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}$$
 by power method Take $X_0 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$. (10)

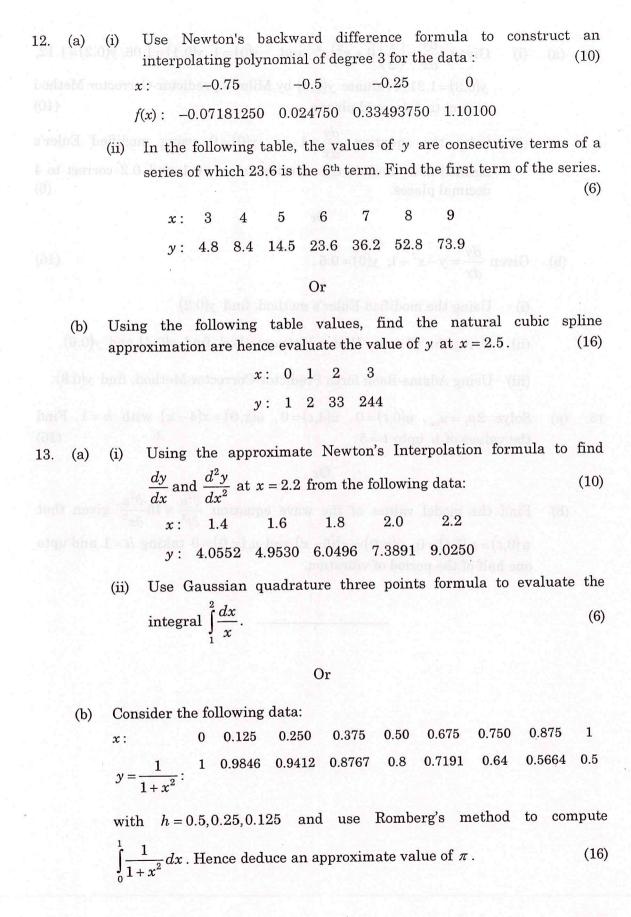
Or

(b) Solve the following system of equations by Gauss-Seidal Method (16)

$$20x + y - 2z = 17$$

$$3x + 20y - z = -18$$

$$2x - 3y + 20z = 25$$



- 14. (a) Given $\frac{dy}{dx} = \left(\frac{1}{2}\right)\left(1+x^2\right)y^2$ and y(0) = 1, y(0.1) = 1.06, y(0.2) = 1.12, y(0.3) = 1.21, evaluate y(0.4) by Milne's predictor-Corrector Method correct to 4 decimal places. (10)
- (ii) Solve the equation $\frac{dy}{dx} = 1 y$, y(0) = 0 using modified Euler's method and tabulate the solutions at x = 0.1 and 0.2 correct to 4 decimal places.

Or

(b) Given
$$\frac{dy}{dx} = y - x^2 + 1$$
, $y(0) = 0.5$. (16)

- (i) Using the modified Euler's method, find y(0.2)
- (ii) Using the 4th order Runge-Kutta method, find y(0.4) and y(0.6).
- (iii) Using Adams-Bash forth Predictor-Corrector Method, find y(0.8).
- 15. (a) Solve $2u_t = u_{xx}$, u(0,t) = 0, u(4,t) = 0, u(x,0) = x(4-x) with h = 1. Find the values of u upto t = 5.

Or

(b) Find the model values of the wave equation $\frac{\partial^2 u}{\partial t^2} = 16 \frac{\partial^2 u}{\partial x^2}$ given that u(0,t) = u(5,t) = 0, $u(x,0) = x^2(5-x)$ and $u_t(x,0) = 0$ taking h = 1 and upto one half of the period of vibration.